

INTEGRAL ERROR REPRESENTATION OF HERMITE INTERPOLATING POLYNOMIALS AND RELATED GENERALIZATIONS OF STEFFENSEN'S INEQUALITY

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Abstract. Some representations of Steffensen's inequality are obtained by using Hermite interpolating polynomials. The obtained representations are used to prove new generalizations of Steffensen's inequality for n -convex functions and to give some bounds for integrals in these representations.

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