

## ANOTHER CHARACTERIZATION OF ORTHOGONALITY IN HILBERT $C^*$ -MODULES

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*Abstract.* We discuss a certain relation related to the Roberts orthogonality in Hilbert  $C^*$ -modules which turns out to be equivalent to the orthogonality with respect to the  $C^*$ -valued inner product. We also describe Hilbert  $C^*$ -modules in which the Birkhoff–James orthogonality coincides with the Roberts orthogonality.

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