

## EXTENSIONS OF LEMOS–SOARES TYPE LOG–MAJORIZATION

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*Abstract.* In this paper, we shall obtain extensions of Lemos-Soares log-majorization via Furuta inequality.

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