

A GROUP-THEORETICAL APPROACH TO EXTENDING THE SCHRÖDINGER-ROBERTSON UNCERTAINTY INEQUALITY

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Abstract. We provide a sufficient condition for expanding the domain in the Schrödinger-Robertson uncertainty inequality for infinitesimal operators derived from a unitary representation of a Lie group.

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