

ON A PROPERTY OF BOX-CONVEX FUNCTIONS

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Abstract. In this paper, we use α -Bernstein operators to solve an open problem related to box-convex functions. Future targeted applications reside in the area of stochastic optimization in problems such as AUC maximization and stochastic programs with chance constraints.

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