

ONE-SIDED CONCENTRATION NEAR THE MEAN OF LOG-CONCAVE DISTRIBUTIONS

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Abstract. A lower bound on the probability $P(0 < X < \delta)$ for all real $\delta > 0$ and all random variables X with log-concave p.d.f.'s such that $EX = 0$ and $EX^2 = 1$ is obtained.

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