

## CHARACTERIZATION OF THE UNBOUNDED BICOMMUTANT OF $C_0(N)$ CONTRACTIONS

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**Abstract.** Recent results have shown that any closed operator  $A$  commuting with the backwards shift  $S^*$  restricted to  $K_u^2 := H^2 \ominus uH^2$ , where  $u$  is an inner function, can be realized as a Nevanlinna function of  $S_u^* := S^*|_{K_u^2}$ ,  $A = \varphi(S_u^*)$ , where  $\varphi$  belongs to a certain class of Nevanlinna functions which depend on  $u$ . In this paper this is generalized to show that given any contraction  $T$  of class  $C_0(N)$ , that any closed (and not necessarily bounded) operator  $A$  commuting with the commutant of  $T$  is equal to  $\varphi(T)$  where  $\varphi$  belongs to a certain class of Nevanlinna functions which depend on the minimal inner function  $m_T$  of  $T$ .

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