

## APPROXIMATE DOUBLE COMMUTANTS IN VON NEUMANN ALGEBRAS AND C\*-ALGEBRAS

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**Abstract.** Richard Kadison showed that not every commutative von Neumann subalgebra of a factor von Neumann algebra is equal to its relative double commutant. We prove that every commutative  $C^*$ -subalgebra of a centrally prime  $C^*$ -algebra  $\mathcal{B}$  equals its relative approximate double commutant. If  $\mathcal{B}$  is a von Neumann algebra, there is a related distance formula.

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