

NONLINEAR MAPS PRESERVING CONDITION SPECTRUM OF JORDAN SKEW TRIPLE PRODUCT OF OPERATORS

H. BENBOUZIANE, Y. BOURAMDANE, M. ECH-CHERIF EL KETTANI
AND A. LAHSSAINI

Abstract. Let $\mathcal{B}(\mathcal{H})$ the algebra of all bounded linear operators on a complex Hilbert space \mathcal{H} with $\dim \mathcal{H} \geq 3$. Let \mathcal{W}, \mathcal{V} be subsets of $\mathcal{B}(\mathcal{H})$ which contain all rank-one operators. Denote by $r_\varepsilon(A)$ the condition spectral radius of $A \in \mathcal{B}(\mathcal{H})$. We determine the form of surjective maps $\phi : \mathcal{W} \rightarrow \mathcal{V}$ satisfying $r_\varepsilon(AB^*A) = r_\varepsilon(\phi(A)\phi(B)^*\phi(A))$ for all A, B in \mathcal{W} , we characterize also the structure of surjective maps $\phi : \mathcal{B}(\mathcal{H}) \rightarrow \mathcal{B}(\mathcal{H})$ with $\sigma_\varepsilon(AB^*A) = \sigma_\varepsilon(\phi(A)\phi(B)^*\phi(A))$ for all A, B in $\mathcal{B}(\mathcal{H})$ where $\sigma_\varepsilon(A)$ is the ε -condition spectrum of an operator A in $\mathcal{B}(\mathcal{H})$.

Mathematics subject classification (2010): Primary 47B49, Secondary 47B48, 47A10, 46H05.

Keywords and phrases: Condition spectra, condition spectral radius, nonlinear Jordan skew triple product preservers.

REFERENCES

- [1] H. BENBOUZIANE, Y. BOURAMDANE, M. ECH-CHERIF EL KETTANI, A. LAHSSAINI, *Nonlinear commutant preservers*, Linear and Multilinear Algebra, (2017), doi:10.1080/03081087.2017.1307915.
- [2] M. BENDAOUD, A. BENYOUNESS, M. SARIH, *Condition spectra of special operators and condition spectra preservers*, J. Math. Anal. Appl. (2017), <http://dx.doi.org/10.1016/j.jmaa.2016.12.022>.
- [3] M. BENDAOUD, A. BENYOUNESS, M. SARIH, *Preservers of pseudo spectral radius of operator products*, Linear Algebra Appl. **489** (2016) 186–198.
- [4] R. BHATIA, P. ŠEMRL, A. R. SOUROUR, *Maps on matrices that preserve the spectral radius distance*, Studia Math. **134** (1999) 99–110.
- [5] A. BOURHIM, T. JARI, J. MASHREIGHI, *Peripheral local spectrum preservers and maps increasing the local spectral radius*, Oper. Matrices **1** (2016) 189–208.
- [6] J. CUI, V. FORSTALL, C. K. LI, V. YANNELLO, *Properties and preservers of the pseudospectrum*, Linear Algebra Appl. **436** (2012) 316–325.
- [7] J. CUI, C. K. LI, Y. T. POON, *Pseudospectra of special operators and pseudospectrum preservers*, J. Math. Anal. Appl. **419** (2014) 1261–1273.
- [8] J. CUI, C. K. LI, AND N. S. SZE, *Unitary similarity invariant function preservers of skew products of operators*, J. Math. Anal. Appl. (2017), <http://dx.doi.org/10.1016/j.jmaa.2017.04.072>.
- [9] M. ECH-CHÉRIF EL KETTANI AND H. BENBOUZIANE, *Additive maps preserving operators of inner local spectral radius zero*, Rendiconti del Circolo Matematico di Palermo **63** (2) (2014) 311–316.
- [10] J. HOU, K. HE, X. ZHANG, *Nonlinear maps preserving numerical radius of indefinite skew products of operators*, Linear Algebra Appl. **430** (2009) 2240–2253.
- [11] A. A. JAFARIAN, A. R. SOUROUR, *Linear maps that preserve the commutant, double commutant or the lattice of invariant subspaces*, Linear and Multilinear Algebra. **38** (1994) 117–129.
- [12] A. KRISHNAN AND S. H. KULKARNI, *Pseudo spectrum of element in Banach algebra*, Oper. Matrices **1** (2017) 263–287.
- [13] S. H. KULKARNI, D. SUKUMAR, *The condition spectrum*, Acta Sci. Math. (Szeged) **74** (2008) 625–641.

- [14] G. K. KUMAR, S. H. KULKARNI, *Linear maps preserving pseudospectrum and condition spectrum*, Banach J. Math. Anal. **6** (2012) 45–60.
- [15] C. K. LI, P. ŠEMRL, N. K. TSING, *Maps preserving the nilpotency of products of operators*, Linear Algebra Appl. **424** (2007) 222–239.
- [16] L. N. TREFETHEN, M. EMBREE, *Spectra and Pseudospectra: The Behavior of Nonnormal Matrices and Operators*, Princeton University Press, Princeton, 2005.