

THE NEW REVERSES OF YOUNG TYPE INEQUALITIES FOR NUMBERS, OPERATORS AND MATRICES

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Abstract. In this note, we give reverses of Young inequality for numbers. Then we establish operator and matrix inequalities corresponding the obtained numerical inequalities.

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