

BREATHER SOLUTIONS ON DISCRETE NECKLACE GRAPHS

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Abstract. We show the existence of breather solutions in a nonlinear Klein-Gordon system on a discrete graph with periodic junctions. The proof is based on the Theorem of Crandall-Rabinowitz.

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