

ON A STEVIĆ–SHARMA TYPE OPERATOR FROM $Q_K(p,q)$ SPACES TO BLOCH-TYPE SPACES

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Abstract. The aim of this paper is to investigate the boundedness and compactness of a Stević-Sharma type operator $T_{\psi_1, \psi_2, \phi}^n$ from $Q_K(p, q)$ and $Q_{K,0}(p, q)$ spaces to Bloch-type spaces and little Bloch-type spaces.

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