

ORDER BOUNDED STEVIĆ-SHARMA OPERATORS BETWEEN WEIGHTED DIRICHLET SPACES

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Abstract. The order bounded Stević-Sharma operators between weighted Dirichlet spaces are characterized, which generalizes the previous result obtained by Lin and his colleagues.

Mathematics subject classification (2020): Primary 47B38; Secondary 30H05, 46E15.

Keywords and phrases: Weighted Dirichlet space, Stević-Sharma operator, order boundedness.

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