Differential
Equations
& Applications
Volume 3, Number 1 (2011), 1–10

ON A CLASS OF ABSTRACT FUNCTIONAL DIFFERENTIAL EQUATIONS INVOLVING ALMOST SECTORIAL OPERATORS

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Abstract. We study the existence of mild solutions for a class of abstract functional differential equations involving almost sectorial operators. A concrete application to delayed partial differential equations is presented.

Mathematics subject classification (2010): 34K30, 35R10, 47D06.
Keywords and phrases: functional differential equations, almost sectorial operator, mild solution, semigroup of growth α.

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Paper DEA-03-01