

## OSCILLATION OF SECOND ORDER NONLINEAR IMPULSIVE DIFFERENTIAL EQUATIONS WITH DEVIATING ARGUMENTS

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*Abstract.* In this paper, we present some new sufficient conditions for the oscillations of all solutions of a second order retarded differential equations with impulses. These results extend the known results for the differential equations without impulses. An example is provided to illustrate our result.

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