

## ASYMPTOTIC BEHAVIOR OF POSITIVE SOLUTIONS OF A LANCHESTER–TYPE MODEL

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*Abstract.* An ordinary differential system, referred to as Lanchester-type model, is treated. We examine how asymptotic behavior of every solution of the system varies according to the initial data. We can show the existence of critical values for initial data.

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