

## ALMOST PERIODIC HOMOGENIZATION OF THE KLEIN–GORDON TYPE EQUATION

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*Abstract.* In this paper, the homogenization problem for the Klein–Gordon type equation is studied in the almost periodic setting. The propagation speed and the potential are spatial and time dependent almost periodically varying functions. One convergence theorem is proved and we derive the macroscopic homogenized model verified by the mean wave function.

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