

## FRACTIONAL DIFFERENCE INEQUALITIES OF OPIAL TYPE AND INITIAL VALUE PROBLEM

G. V. S. R. DEEKSHITULU AND J. JAGAN MOHAN

*Abstract.* In this paper some discrete Opial type inequalities of fractional order are established and using these inequalities of Opial type, a bound to the solution of a fractional initial value problem is obtained.

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