

ON CONTROLLABILITY OF LINEAR AND NONLINEAR FRACTIONAL INTEGRODIFFERENTIAL SYSTEMS

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Abstract. In this article we investigate the controllability problem of linear and nonlinear fractional integrodifferential systems. We justify the controllability concepts on a fractional integrodifferential linear system, and use results, as well as Schauder's fixed point theorem, to obtain the controllability of the corresponding nonlinear system. Some applications are introduced to explain the theoretic parts.

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