

NONLINEAR FRACTIONAL DIFFERENTIAL EQUATIONS WITH m -POINT INTEGRAL BOUNDARY CONDITIONS

TUGBA SENLIK CERDIK, NUKET AYKUT HAMAL AND FULYA YORUK DEREN

Abstract. In this paper, we consider the existence and uniqueness of solution for a fractional order differential equation involving the Riemann-Liouville fractional derivative. By applying some standard fixed point theorems, we obtain new results on the existence and uniqueness of solution.

Mathematics subject classification (2010): 34B10, 34B18.

Keywords and phrases: Integral boundary condition, fractional differential equation, fixed point theory.

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