

EXACT EVALUATION OF SOME HIGHLY OSCILLATORY INTEGRALS

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Abstract. In this note a general result is proved that can be used to evaluate exactly a class of highly oscillatory integrals. The result can also be used to give a procedure to numerically evaluate some oscillatory integrals.

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