

ON RATIONAL APPROXIMATION OF FUNCTIONS IN REARRANGEMENT INVARIANT SPACES

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Abstract. Some direct theorems for polynomial and rational approximation of functions in the complex plane are proved.

Mathematics subject classification (2010): 30E10, 41A20, 41A25, 46E30.

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