

ORDER IDEAL LIMIT POINTS AND A GENERALIZED BOLZANO–THEOREM

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Abstract. In this paper we extend the concept of I-limit points and I-cluster points in a linearly ordered metric additive system and study the notion of *OI*-limit points and *OI*-cluster points and also establish a generalization of Bolzano-Weierstrass theorem connected to a bounded sequence.

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