

## GENERALIZED WEIGHTED COMPOSITION OPERATORS FROM WEIGHTED BERGMAN SPACES INTO ZYGMUND–TYPE SPACES

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*Abstract.* The boundedness and the compactness of generalized weighted composition operators from weighted Bergman spaces into Zygmund-type spaces are investigated in this paper. Moreover, we give some estimates for the essential norm of these operators.

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