

FURTHER RESULTS ON VALUE DISTRIBUTION OF L-FUNCTIONS

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Abstract. With the aid of weighted sharing we study the uniqueness of meromorphic functions concerning nonlinear differential polynomials that share a nonzero polynomial with the same of L-functions. Our results in the paper will improve, extend a results due to Fang Liu, Xiao-Min Li and Hong-Xun Yi [5].

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