

HYPERSTABILITY OF A MIXED TYPE CUBIC–QUARTIC FUNCTIONAL EQUATION IN ULTRAMETRIC SPACES

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Abstract. In this paper, we present the hyperstability results of a mixed type cubic–quartic functional equations in ultrametric Banach spaces.

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