

ON WEIGHTED β -ABSOLUTE CONVERGENCE OF DOUBLE FOURIER SERIES

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Abstract. In this paper, we obtain a sufficient condition for the weighted β -absolute convergence ($0 < \beta < 2$) of the double Fourier series of a function f of (ϕ, ψ) - (Λ^1, Λ^2) -bounded variation.

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