

## IDEAL STATISTICALLY LIMIT POINTS AND IDEAL STATISTICALLY CLUSTER POINTS OF TRIPLE SEQUENCES OF FUZZY NUMBERS

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*Abstract.* In this paper we extend the notions of ideal statistical limit points and ideal statistical cluster points for a sequence of fuzzy numbers. We introduce the notions ideal statistical limit points and ideal statistical cluster points of a triple sequence of fuzzy numbers, and give some correlation theorem.

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