

## LOCATION OF ZEROS OF LACUNARY-TYPE POLYNOMIALS IN ANNULAR REGIONS

IRFAN AHMAD WANI\*, MOHAMMAD IBRAHIM MIR AND ISHFAQ NAZIR

*Abstract.* In this paper, we place certain conditions on the real and imaginary parts of the coefficients of a lacunary-type polynomial and find the annular regions containing all the zeros of a lacunary-type polynomial.

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