

A NOTE ON A FAMILY OF LOG-INTEGRALS

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Abstract. A family of log-integrals with three parameters is analyzed. In particular, some difficult integrals are evaluated exactly using the derivatives of the Gamma function.

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