

## SQUARE-FREE FACTORIZATION OF MIXED TRIGONOMETRIC-POLYNOMIALS

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*Abstract.* This paper proposes a procedure to square-free factorization of mixed trigonometric-polynomials and some examples are presented to show the effectiveness of the algorithm.

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