

## ON STATISTICAL CONVERGENCE OF SET SEQUENCES IN FUZZY ANTI-NORMED LINEAR SPACE

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*Abstract.* The current study aims to investigate the notion of set sequences in the context of fuzzy anti-norm linear space. We define the fuzzy  $\alpha$ -anti Wijsman convergence, fuzzy  $\alpha$ -anti Wijsman statistical convergence, and fuzzy  $\alpha$ -anti Hausdorff statistical convergence, for  $0 < \alpha < 1$ , and presented some novel examples to support the definitions. Additionally, some original theorems which show how the notions are connected, are established.

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