

## ON WEIGHTED SIMPSON TYPE INEQUALITIES AND APPLICATIONS

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*Abstract.* In this paper we establish some weighted Simpson type inequalities and give several applications for the  $r$  – moments and the expectation of a continuous random variable. An approximation for Euler’s Beta mapping is given as well.

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