

SUPER-STABILITY AND STABILITY OF THE EXPONENTIAL EQUATIONS

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Abstract. In this paper, we introduce the concepts of super-stability, stability, δ -Ger-stability of the exponential equation of an operator from a normed space into a normed algebra. By using some results due to J. Baker and R. Ger, we obtain some new conclusions about these stabilities.

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