

INEQUALITIES FOR TERMINATING ${}_r+1\phi_r$ AND APPLICATIONS

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Abstract. In this paper, we use the q -binomial formula to establish two inequalities for the terminating basic hypergeometric series ${}_r+1\phi_r$. Applications of the inequalities are also given.

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