

A WEAK POINCARÉ-SOBOLEV INEQUALITY FOR FUNCTIONS IN MORREY SPACES

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Abstract. We prove a weak Poincaré-Sobolev type inequality for a function belonging to Morrey spaces with respect to a Hausdorff content.

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