

THE BEST CONSTANT IN A GEOMETRIC INEQUALITY RELATING MEDIAN, INRADIUS AND CIRCUMRADIUS IN A TRIANGLE

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Abstract. In this paper, the authors give a refinement of the inequality associated with the medians, inradius and circumradius in a triangle by making use of certain analytical techniques for systems of nonlinear algebraic equations.

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