

SOME INEQUALITIES FOR THE SPECTRAL RADIUS OF THE HADAMARD PRODUCT OF TWO NONNEGATIVE MATRICES

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Abstract. In this paper, we propose some sharper upper bounds for the spectral radius of the Hadamard product of two nonnegative matrices. The results involve the directed graph of the Hadamard product of associated matrices.

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