

REMARK ON OZEKI INEQUALITY FOR CONVEX POLYGONS

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Abstract. This paper gives proof of a discrete inequality that represents Ozeki's inequality for convex polygons and its converse. The proof is based on determining eigenvalues of one nearly tridiagonal symmetric matrix.

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