

SOME NEW OSTROWSKI-TYPE BOUNDS FOR THE ČEBYŠEV FUNCTIONAL AND APPLICATIONS

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Abstract. Some new inequalities of Ostowski-type for the Čebyšev functional and applications for Taylor's expansion and generalised trapezoid formula are pointed out.

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