

A NOTE ON THE NEUMAN–SÁNDOR MEAN

HUI SUN, TIEHONG ZHAO, YUMING CHU AND BAOYU LIU

Abstract. In this article, we present several best possible lower bounds for the Neuman–Sándor mean in terms of the geometric combinations of harmonic and quadratic means, geometric and quadratic means, harmonic and contraharmonic means, and geometric and contraharmonic means.

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