

EMBEDDINGS BETWEEN WEIGHTED LOCAL MORREY-TYPE SPACES AND WEIGHTED LEBESGUE SPACES

R. CH. MUSTAFAYEV AND T. ÜNVER

Abstract. In this paper, the embeddings between weighted local Morrey-type spaces and weighted Lebesgue spaces are investigated.

Mathematics subject classification (2010): 42B35, 47B38.

Keywords and phrases: local Morrey-type spaces, weighted Lebesgue spaces, Hardy-type inequalities.

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