INEQUALITIES FOR DUAL QUERMASSINTEGRALS
OF THE p–CROSS–SECTION BODIES

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Abstract. Gardner and Giannopoulos defined the p-cross-section body $C_p K$ ($p > -1$) of convex body K in Euclidean space $\mathbb{E}^n$. In this paper, we obtain inequalities for dual quermassintegrals of the p-cross-section body $C_p K$. Further, two monotonic inequalities concerning the $C_p K$ are given.

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