

A NOTE ON THE BEST CONSTANTS IN SOME HARDY INEQUALITIES

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Abstract. The sharp constants in Hardy type inequalities are known only in a few cases. In this paper we discuss some situations when such sharp constants are known, but also some new sharp constants are derived both in one-dimensional and multi-dimensional cases.

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