

## A SHORT EXTENSION OF TWO OF SPIRA'S RESULTS

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*Abstract.* Two inequalities concerning the symmetry of the zeta-function and the Ramanujan  $\tau$ -function are improved through the use of some elementary considerations.

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