

MULTI-PARAMETER GENERALIZATION OF RADO-POPOVICIU INEQUALITIES

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Abstract. By using methods on the theory of majorization, new generalizations of Rado's inequality and Popoviciu's inequality which involves multi-parameter are established.

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