

REMARK ON ORDINARY AND RANDIĆ ENERGY OF GRAPHS

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Abstract. Let G be an undirected simple graph with n vertices and m edges. Denote with $|\lambda_1| \geq |\lambda_2| \geq \dots \geq |\lambda_n|$ and $|\rho_1| \geq |\rho_2| \geq \dots \geq |\rho_n|$ absolute eigenvalues and Randić eigenvalues of G arranged in non-increasing order, respectively. Upper bound of graph invariant $E(G) = \sum_{i=1}^n |\lambda_i|$, and lower and upper bounds of invariant $RE(G) = \sum_{i=1}^n |\rho_i|$ are obtained in this paper.

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