

## ON D'AURIZIO'S TRIGONOMETRIC INEQUALITY

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*Abstract.* We offer new proof of the recent sharp trigonometric inequality  $\cos x / \cos(x/2) \geq 1 - 4x^2/\pi^2$  for  $x \in (0, \pi/2)$ , discovered by Jacopo D'aurizio [1]. The converse inequality, as well as sharp analogous inequalities are pointed out, too.

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### REFERENCES

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