

REFINEMENTS OF THE CAUCHY–SCHWARZ INEQUALITY FOR τ –MEASURABLE OPERATORS

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Abstract. In this paper, we present the convexity of certain functions in noncommutative symmetric space generalizing the previous result of Hiai and Zhan. As an application, we gave some refinements of the Cauchy-Schwarz inequality for τ -measurable operators by using some integration techniques.

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