

L^r CONVERGENCE FOR WEIGHTED SUMS OF EXTENDED NEGATIVELY DEPENDENT RANDOM VARIABLES

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Abstract. In this paper, we establish some results on L^r convergence for weighted sums of extended negatively dependent random variables under r -th uniform integrability. The results obtained in the paper generalize some corresponding ones for independent random variables and some dependent random variables.

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